

# Lecture 1: Heterogeneity, the Net Worth Channel, and the Financial Accelerator

Alp Simsek

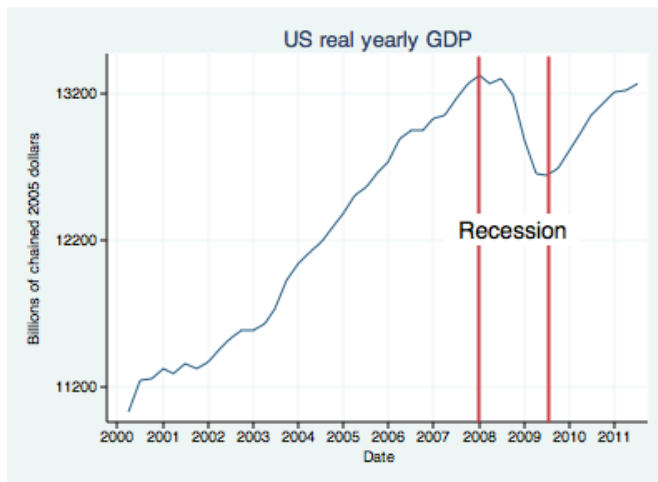
June 20, 2014

# Roadmap

- 1 Course introduction
- 2 Frictionless benchmark:  $q$  theory of investment
- 3 Investment with frictions
- 4 Net worth channel
- 5 Financial accelerator

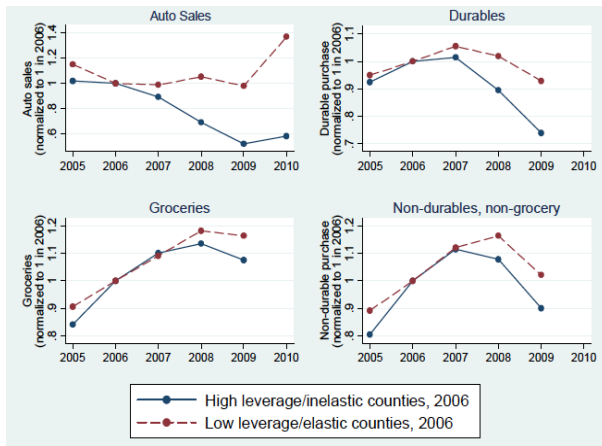
- **Instructor:** Alp Simsek.
- **Readings:** In the syllabus.
- **Textbooks:** None required but Tirole's "The Theory of Corporate Finance" is a useful reference.
- Course is accelerated: 9 lectures in 3 days!

# Motivation for the course: The recent recession



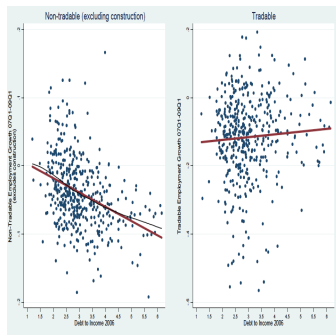
# Evidence suggests financial frictions

- Mian, A., K. Rao, and A. Sufi (2011), "Household balance sheets, consumption, and the economic slump."



# Evidence suggests demand-side effects

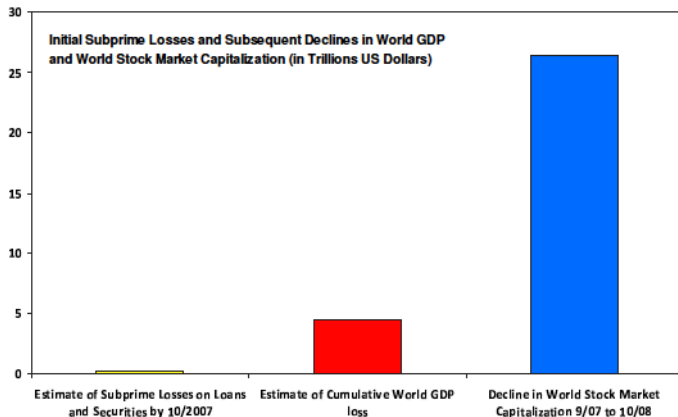
- Mian A. and A. Sufi (2011), “What explains high unemployment? The aggregate demand channel.”



- Cross-county effects show up in non-tradable industries (restaurants, department stores etc.) but not in tradable industries (manufacturing, software etc.).

# Evidence suggests amplification

- Blanchard, O. (2009), "The crisis: Basic mechanisms and appropriate policies."



Source: IMF Global Financial Stability Report; World Economic Outlook November update and estimates; World Federation of Exchanges.

- 1 Borrowing constraints and investment (3 lectures)
  - Limited pledgeability, dynamics, financial accelerator, precautionary savings, underinsurance, crises.
- 2 Financial crises and amplification mechanisms (3 lectures)
  - Leverage, fire sales, bank runs.
- 3 Borrowing constraints and recessions (3 lectures)
  - Consumption, demand channel, nominal rigidities, liquidity trap.



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# Consider the neoclassical investment theory (q theory)

- Economy with periods,  $t \in \{0, \dots, \infty\}$ , single consumption good, and one factor of production (capital).
- State  $s_t \in S = \{s^1, \dots, s^n\}$  follows a Markov chain.
- Consider a firm with technology  $y_t = s_t f(k_t)$ .
  - $k_t$  is installed capital and  $s_t$  captures productivity.
  - $f(\cdot)$  is a neoclassical function with standard properties.
- **Adjustment costs:** Investing  $i_t = \iota_t k_t$  costs the firm  $i_t (1 + \frac{1}{2}\phi\iota_t)$ . (CRS)
- **Asset pricing:** Stochastic discount factor  $m_{t,t+1} = m(s_t, s_{t+1})$ .
  - For simplicity assume  $m(s_t, s_{t+1}) = \beta$ .
  - Everything generalizes as long as firm takes  $m(\cdot)$  as given.

# Firm's net profits in a period might be negative

- The firm's net profit in a period is given by:

$$\pi_t = \underbrace{R_t k_t}_{\text{revenues}} - \underbrace{\iota_t k_t \left(1 + \frac{1}{2} \phi \iota_t\right)}_{\text{investment costs}}$$

- Firm chooses investment policy to maximize:

$$V(k_0, s_0) = \max_{\{\iota_t, k_{t+1}\}_{t=0}^{\infty}} E \left[ \sum_{t=0}^{\infty} \beta^t \pi_t \mid s_0 \right], \quad (1)$$

s.t.  $k_{t+1} = (1 - \delta) k_t + \iota_t k_t$  for each  $t, s_t$ .

- Any positive NPV investment is undertaken (by definition).**

# Firm's problem in recursive form

Firm's problem is recursive. Bellman:

$$V(k, s) = \max_{\iota, k'} Rk - \iota k \left( 1 + \frac{1}{2} \phi \iota \right) + E [\beta V(k', s') \mid s]$$

s.t.  $k' = (1 - \delta)k + \iota k$ .

- Define  $q^m(k, s)$  as the marginal value of new capital (the Lagrange multiplier on the constraint).
- This is known as **Tobin's (marginal) q**.
- What is the economic interpretation of  $q^m$ ?

# Investment is increasing in marginal $q$

- FOC for  $\iota$  gives:

$$1 + \phi\iota = q^m(k, s).$$

- After rewriting, we have:

$$\iota(k, s) = \frac{i(k, s)}{k} = \frac{q^m(k, s) - 1}{\phi}. \quad (2)$$

**Marginal  $q$  is a sufficient statistic for investment (controlling for  $k$  and adjustment costs).**

- Future profits, discount rates etc are all summarized in marginal  $q$ .
- Problem: Marginal  $q$  is not observable....

# Under some conditions, marginal $q$ equals average $q$

- Define the average  $q$  as the ex-dividend value of installed capital:

$$q(k, s) = \frac{E[\beta V(k', s') \mid s]}{k'}. \quad (3)$$

- Note problem (1) is linear, i.e.,  $v(k, s) = v(s)k$  for some  $v(\cdot)$ .
- Using this observation and taking the FOC for  $k'$ , we then obtain:

$$q^m(k, s) = E[\beta v(s') \mid s] = q(k, s).$$

**Intuition:** CRS implies new capital is equally valuable as installed capital (See Hayashi, 1982). Useful starting point.

# Summary: $q$ is a sufficient statistic for investment

- Bringing back Eq. (2), we have:

$$\frac{i(k, s)}{k} = \frac{q(k, s) - 1}{\phi}.$$

**Average  $q$  is a sufficient statistic for investment.**

- **Implication:** Eq. (2) now becomes **testable**. How?

# Alternative to q theory: Cash flows might matter

Towards developing an alternative against which to test q theory, suppose the firm chooses to finance-as-you-go (no asset accumulation).

- If  $\pi_t > 0$ , firm pumps out cash in period  $t$  (dividends etc.).
- If  $\pi_t < 0$ , firm borrows in period  $t$  (issues claims, takes loan etc.).



## Alternative to q theory: Cash flows might matter

- Now suppose the firm faces an additional **borrowing constraint**:

$$\pi_t \geq 0 \text{ for each } t \text{ and } s_t.$$

To highlight the differences with q theory:

- Suppose shocks are iid so that  $q^m = \beta E[v(s') | s]$  independent of  $s$ .
- Consider a state with low current cash flows,  $s \simeq 0$ .
- What happens to investment in the frictionless benchmark?
- What happens in the alternative with borrowing constraints?

# First pass: horse race between $q$ and cash flows

Collecting the observations, we have:

- **Frictionless: Average  $q$  is a sufficient statistic for investment.**
- **Alternative: Current cash flows also matter for investment.**

Fazzari, Hubbard, Petersen (1988) run the panel regression:

$$\left(\frac{i}{k}\right)_{j,t} = q_{j,t}\beta_1 + \left(\frac{\text{cash flow}}{k}\right)_{j,t} \beta_2 + \varepsilon_{j,t},$$

for the US manufacturing firms.

- $q$  theory suggests  $\beta_1 > 0$  and  $\beta_2 \simeq 0$ .
- In the data:  $\beta_2 > 0$  and  $\beta_1 \simeq 0$ .

# FHP: $q$ is generally insignificant, cash flows are significant

**Table 4. Effects of  $Q$  and Cash Flow on Investment, Various Periods, 1970–84<sup>a</sup>**

<i>Independent variable and summary statistic</i>	<i>Class 1</i>	<i>Class 2</i>	<i>Class 3</i>
		1970–75	
$Q_{it}$	-0.0010 (0.0004)	0.0072 (0.0017)	0.0014 (0.0004)
$(CF/K)_{it}$	0.670 (0.044)	0.349 (0.075)	0.254 (0.022)
$\bar{R}^2$	0.55	0.19	0.13

Class 3 retain less earnings (pay more dividends) than class 1 firms.

## Second pass: exogenous shocks to cash flows

- FHP calculate  $q$  using the firm's market value.
- Perhaps  $q$  is mismeasured (e.g., market sentiment) and  $CF$  is a better predictor of future profits.
- Another alternative is to try to find an exogenous variation in  $CF$ .
- Blanchard, Lopez-de-Silanes, and Shleifer (1994), Lamont (1997), Rauh (2006)...

Results generally suggest cash flows/internal funds also matter.

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## **Alternative:** Investment with financial frictions:

- Asymmetric information (see Stein, 2003):
  - Moral hazard: Borrowers'/managers' unobserved effort/project choice.
  - Adverse selection: Borrowers' private information.
- Incomplete contracts and control (see Hart, 2001):  
Not all contingencies can be foreseen.
- Commitment and collateral:  
Borrowers might default. How to enforce payment.

We start with asymmetric information but emphasize mechanisms that are general across frictions.

- Normative analysis usually depends on nature of frictions.

Key implication: **Limited pledgeability** and **borrowing constraints**:

- 1 **Net worth channel** in investment.
- 2 **Financial shocks** matter for macro outcomes.
- 3 Financial shocks exacerbate and propagate other shocks (**financial accelerator**).

**Next:**

- Holmstrom and Tirole's moral hazard model to illustrate 1 and 2.
- A variant of Bernanke and Gertler (1989) to illustrate 3.

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# Financial frictions: Key feature is heterogeneity

- Two dates  $t \in \{0, 1\}$ , and a single consumption good (dollar).
- Two types of agents: financiers (F) and potential investors.  
We refer to the latter as an entrepreneur (E), but think more broadly.
- Both types with linear preferences  $U = C_1 + \beta C_2$ .
- F's have large endowment of dollars. Competitive loan market.  
Ensures the interest rate is  $1 + r \equiv 1/\beta$ . Will endogenize this later.

**Key modeling feature is heterogeneity. Focus is on Es.**

# Financial frictions: Key feature is heterogeneity

- One E with access to a fixed scale project:  
Investing 1 dollar (normalized) at date 0 yields output at date 1.
- E has endowment (net worth)  $N$  dollars at date 0.  
Assume  $1 > N$  so that project needs financing.
- E has no endowment at date 1.
- E has **limited liability** at both dates:  $C_1 \geq 0$  and  $C_2 \geq 0$ .

**Fundamental problem is a mismatch of ideas and resources.**

## Moral hazard: E can misbehave

- Two states at date 1: Project either succeeds and yields  $\frac{R}{p_H}$ , or fails and yields 0. (We normalize  $R$  to be the average return).
- **Moral hazard:** E may shirk and choose a different project.
- Two versions of the project:

Project	Good	Bad
Private benefit	0	$B > 0$
Prob. of success	$p_H$	$p_L < p_H$

- Project is positive NPV iff E behaves, that is:

$$\beta \left( p_L \frac{R}{p_H} + B \right) < 1 < \beta R.$$

**Information friction: E's project choice is not observable to Fs.**

# A contract specifies the division of output

A contract transfers  $1 - N$  to E and specifies the division of output in case of success subject to:

- **Resource constraints (RC):**

$$\frac{R^F}{p_H} \text{ and } \frac{R^E}{p_H} \geq 0, \text{ with } R^F + R^E \leq R.$$

- **F's participation constraint (PC):**

$$1 - N = \beta \left( p_H \frac{R^F}{p_H} \right).$$

- **E's incentive constraint (IC):**

$$p_H \frac{R^E}{p_H} \geq p_L \frac{R^E}{p_H} + B \text{ which implies } R^E \geq \frac{p_H}{\Delta p} B.$$

**For good management, E must have “skin in the game.”**

# Key implication: Limited pledgeability (LP)

- Combining (RC) with (IC), we obtain a **limited pledgeability (LP)** constraint:

$$R^F \leq \rho \equiv R - \frac{p_H}{\Delta p} B.$$

Here,  $\rho < R$  is the (expected) **pledgeable output**.

- LP is the main difference from the frictionless benchmark.
- It is also the **common denominator of various frictions**:
  - Adverse selection generates a similar effect. Why?
  - Incomplete contracts generate a similar effect. Why?
  - Commitment/collateral generates a similar effect. Why?

# LP generates a borrowing constraint...

Combining (LP) with (PC), we obtain a **borrowing constraint (BC)**:

$$1 - N \leq \beta\rho.$$

E can only borrow up to the pdv of the **pledgeable output**.

- Some positive NPV projects may not be undertaken.
- Whether or not this happens depends on E's net worth.

**Net worth channel:** Rewire the inequality as:

$$N \geq \bar{N} = 1 - \beta\rho.$$

- E's with sufficient (liquid) net worth receive financing and invests.
- E's with insufficient net worth ( $N < \bar{N}$ ) are denied credit.

**Credit rationing:** When prices have incentive (or information) effects, credit markets may clear with quantities rather than prices.

- E's with  $N < \bar{N}$  are willing to promise a higher rate,  $R^F$ . But F's don't accept this because of adverse incentives.

# Holmstrom-Tirole model: Flexible scale version

- It is also useful to consider another variant of the model. (Building block for many other models. See Tirole's book).
- Slight difference for investment technology: **Scale is flexible.**
- Investing  $I$  units in the project yields  $\frac{R}{p_H} I$  units in case of success and 0 units in case of failure.
- Two versions of the project:

Project	Good	Bad
Private benefit	0	$BI > 0$
Prob. of success	$p_H$	$p_L < p_H$

Private benefit also scales up with investment (for simplicity).



## E chooses the investment level and a feasible contract

- E with net worth  $N$  invests  $I \geq N$ . Now choice variable.
- As before, (IC) and (RC) lead to **(LP)**

$$R^F \leq \rho \equiv R - \frac{p_H B}{\Delta p}.$$

- Combined with (PC), generates a **(BC)**:

$$I - N \leq \beta \rho I.$$

- **E's problem:** Choose  $I \geq N$  that maximizes her expected payoff,  $\beta R I - (I - N)$ , subject to (BC).

# Investment depends on E's net worth

- Assume the following (why?):

$$\beta\rho < 1 < \beta R.$$

- Then, E invests up to the maximum possible scale:

$$I = \frac{N}{1 - \beta\rho}.$$

- This aggregates nicely over all E's:

$$I^{agg} = \frac{N^{agg}}{1 - \beta\rho}.$$

Aggregate investment depends on the **net worth of Es** in the economy.

① **Financial shocks** that lower E's net worth lower investment:

- Shock to Es cash flows. Consistent with earlier evidence.
- Shocks to Es assets, e.g., subprime shock.

② **Heterogeneity** and **distribution of wealth** matters.

- Transfer of wealth from Es to Fs lower investment. E.g., nominal contracts and deflation (Fisher).

None of these effects would be present in a rep. agent framework.

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# Net worth channel also has dynamic implications

- Bernanke and Gertler (1989): Net worth channel in a dynamic setting.
- **Financial accelerator:** Amplification and propagation of other (business cycle) shocks.
  - E's net worth likely to be procyclical (less solvent during bad times).
  - A recession will erode net worth, which in turn will reduce investment and exacerbate the recession (and vice versa for a boom).
- **Next:** H-T model in a dynamic macro environment to illustrate the mechanism.

# Consider a standard OLG model

- Consider an OLG economy with a single consumption good (dollars) and two factors: capital and labor.
- Generation  $t$  individuals live for two periods. Continuum of 1 total.
- E's and F's with prefs:  $C_{t,1} + \frac{1}{1+r} C_{t,2}$ .
- Production technology:  $A_t F(K_t, L_t)$ .
  - Suppose (for simplicity)  $A_t$  is i.i.d. with mean  $\bar{A}$ .
  - Suppose (for simplicity) capital depreciates fully after use.
- Labor is supplied inelastically by the young,  $L_t = 1$ .
- Factor markets are competitive:

$$R_t = A_t F_K(K_t, 1) \text{ and } w_t = A_t F_L(K_t, 1). \quad (4)$$

# Benchmark: Equilibrium without frictions

- Start with a benchmark with no frictions.
- Young E's have access to an investment technology:  $I_t$  dollars invested generates  $\frac{I_t}{p_H}$  units of **capital** date  $t + 1$  with prob.  $p_H$  (0 otherwise).
- Continuum with no aggregate uncertainty implies:

$$K_{t+1} = I_t.$$

- Equilibrium capital found from:

$$\underbrace{1 + r = E[R_{t+1}]}_{\text{intuition?}} = \bar{A}F_K(K^*, 1).$$

- Note that  $K_{t+1} = K^*$  is independent of  $A_t$ .

**Without frictions, temporary productivity shocks have no effect on investment.**

# Introduce heterogeneity and frictions

- Suppose E's have mass  $\eta$ , and F's have mass  $1 - \eta$ .
- E's and F's net worth is their labor income:

$$N_t = \eta w_t \text{ and } N_t^F = (1 - \eta) w_t. \quad (5)$$

**E's net worth is endogenous.**



# E's investment technology is subject to moral hazard

- Next suppose E's are subject to moral hazard as in H-T:

Project	Good	Bad
Private benefit	0	$BI_t$ dollars.
Prob. of success	$p_H$	$p_L < p_H$

- In equilibrium, good project is implemented. Still no uncertainty:

$$K_{t+1} = I_t. \quad (6)$$

# E's contract choice is isomorphic to the earlier model

- E's expected return from success:  $E[R_{t+1}] \frac{I_t}{PH} = \bar{A}F_K(K_{t+1}, 1) \frac{I_t}{PH}$ .
- Her private benefit:  $BI_t$ .
- Given  $N_t$ , E chooses the contract  $(I_t \geq N_t, R_{t+1}^E, R_{t+1}^F)$  to maximize her payoff subject to IC and PC:

$$R_{t+1}^E + R_{t+1}^F = E[R_{t+1}].$$

(Distribution of  $R^E$  and  $R^F$  across  $A$ -shocks does not matter since agents are risk-neutral. Will come back to this.)

- E's problem is the same as before with  $E[R_{t+1}]$  replacing  $R$ .

# Definition of dynamic equilibrium

## Definition

Given the initial capital level  $K_0$ , a dynamic equilibrium is a collection of factor allocations  $\{K_t, L_t = 1\}_{t=0}^{\infty}$ , prices  $\{R_t, w_t\}_{t=0}^{\infty}$ , and contracts  $\{I_t, R_{t+1}^E, R_{t+1}^F\}_{t=0}^{\infty}$  such that:

- 1 Factor markets clear [cf. Eq. (4)] and the agents' net worths are given by (5).
- 2 Es in each period  $t$  make their investment and contract decisions optimally.
- 3 Capital evolves according to (6).

Make parametric assumptions such that:

$$\rho_t \equiv E_t [R_{t+1}] - \frac{\rho_H B}{\Delta p} < 1 + r < E_t [R_{t+1}] \text{ for each } t. \quad (7)$$

# Investment is the solution to a fixed point problem

- From the earlier analysis, we have:

$$K_{t+1} = \frac{N_t}{1 - \rho_t / (1 + r)}.$$

- Plugging in the definition of  $\rho_t$  from (7), and using  $E[R_{t+1}] = \bar{A}F_K(K_{t+1}, 1)$ , we have:

$$K_{t+1} = \frac{N_t}{1 - \left( \bar{A}F_K(K_{t+1}, 1) - B \frac{p_H}{\Delta p} \right) / (1 + r)}.$$

- Under regularity conditions, there exists a unique  $K^{next}(\cdot)$  such that  $K_{t+1} = K^{next}(N_t)$ . The function  $K^{next}(N_t)$  is increasing in  $N_t$ .
- Check these for the Cobb-Douglas case,  $F(K, 1) = K^\alpha$ .

# Financial accelerator and the propagation of shocks

- Plugging in  $N_t = \eta A_t F_L(K_t, 1)$  we obtain:

$$K_{t+1} = K^{next}(\eta A_t F_L(K_t, 1)).$$

- **Amplification:**  $K^{next}$  is increasing in  $A_t$ .  
Temporary shocks reduce investment and exacerbate the recession.
- **Propagation:**  $K^{next}$  is increasing in  $A_t$  and  $K_t$ .

Temporary shocks have long lasting effects:

$$A_t \downarrow \implies K_{t+1} \downarrow \implies K_{t+2} \downarrow \dots$$

**Intuition:** Net worth channel:

$$A_t \downarrow \implies N_t \downarrow \implies K_{t+1} \downarrow \implies N_{t+1} \downarrow \implies K_{t+2} \downarrow \dots$$

- Endogenizing E's net worth through wages not very compelling. Most investment done by old firms, not entrants.
- The mechanism is more general and applies for longer-horizon firms: Low  $A_t \implies$  Low profits and low net worth  $\implies$  Lower investment  $\implies$  Low profits and net worth in the future...
- But longer horizons generate a demand for hedging aggregate shocks ( $A$ -shocks here). Will come back to this.

# Taking stock: Heterogeneity and net worth channel

- Cash flows/internal funds seem to matter for investment.
- Alternative to q theory: Investment with financial frictions:
- Common ingredients:
  - **Heterogeneity** ( $E_s$  and  $F_s$ ).
  - **Limited pledgeability**.
- Common implications:
  - **Borrowing constraints** and **net worth channel** in investment.
  - **Financial shocks** affect investment.
  - Financial frictions **accelerate** other shocks.

**Next time:** Dynamics and the precautionary savings motive.